# Classification Event Sequences via Compact Big Sequence 

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#### Abstract

The sequence classification is considered as one of the important data mining tasks. It has a broad range of real-world applications such as bioinformatics, medicine, finance, and abnormal detection. In the literature, several algorithms have been proposed for sequence classification from different aspects. Existing algorithms can be partitioned into three types feature-based, distance-based, and model-based algorithms. In particular, the feature-based algorithms are widely applied for the sequence classification in the literature. In this paper, we propose a new event sequence classification method that based on the idea of the compact big sequence (BigSeq). Our classification method called CBigSeq. It is featurebased method where the features are the used Big Sequences in our model. To evaluate CBigSeq, we compare it with the feature-based method, SeqDT (the state-of-the-art sequence classification algorithm). Our performance study shows that CBigSeq can achieve better performance than SeqDT with respect to classification accuracy, total response time, and count of utilized patterns.


Keywords: Event Sequences, Sequence Classification, Big Sequence, Classification Accuracy

## 1. INTRODUCTION

The sequence classification is considered an essential data mining task. The sequence classification problem is defined as learning a sequence model to get a class label for the new sequence [1]. Sequence classification has many applications such as bioinformatics, health sciences, medicine, finance, and abnormal detection. For example, in finance, we classify sequence data in a bank to combat money laundering [2]. In bioinformatics, protein sequences are added in large repositories daily. To classify these sequences, we search for sequences that have a similar function. When novel sequence added to these repositories, we compared it with current sequences to predict the category of the novel sequence. In information retrieval, we want to classify the documents into distinct topic categories [3].

There are many challenges should be copied to develop a new algorithms for sequence classification. Now we discuss these challenges. In the first challenge, many algorithms take the input sequence data as a vector of features. Unfortunately, non explicit features in sequence data are existed. In the second challenge, the feature selection step is not trivial task. Finally, in
the third challenge, due to the lack of explicit features, we cannot construct an interpretable models.

In the literature, several algorithms have been proposed for sequence classification to address the previous challenges. Existing algorithms can be partitioned into three types (feature-based, distancebased, and model-based algorithms). In this paper, we focus on the feature-based algorithms. In feature-based algorithms, the input data sequence is represented by a vector of features. Thereafter, the classification methods such as Naive Bayes, k-nearest neighbours, decision trees can be used. More details about the feature-based algorithms are listed in Section 3.

In this paper, we propose a novel algorithm called CBigSeq for event sequence Classification that based on our big sequence method (BigSeq) [4]. First, to construct our model, we divide the training sequences into subsets based on the class label. In other words, if we have $m$ distinct class label then we divide the training sequences into m subsets. Thereafter, we construct BigSeq for each subset of sequences. Now, we have $m$ big sequences (BigSeqs) which will represent our model. Finally, we classify the new coming sequence based on the current $m$ BigSeqs. Our
experiments on three real datasets show that CBigSeq has the best performance in most cases compared to the state-of-the-art algorithm, SeqDT [5], in terms of classification accuracy, total response time, and count of utilized patterns.

Organization. This paper is organized as follows. Section 2 reports the preliminary concepts. Section 3 presents the related work. Section 4 discusses the proposed algorithm. Section 5 lists the experimental results. Finally, Section 6 concludes the paper.

## 2. PRELIMINARY CONCEPTS

Let $\sigma$ be a set of $n$ distinct events. Event sequence $V=$ $\left\langle v 1, v 2, \ldots, v h>\right.$ over $\sigma$ is ordered list such that $v_{i} \in$ $\sigma$. Event sequence $U=\left\{u_{1}, u_{2}, \ldots, u_{g}\right\}$ is subsequence of the event sequence $V$ if there are $g$ integers $\left(j_{1}, j_{2}, \ldots\right.$, $j_{g}$ ) such that $l \leq j_{1}<j_{2}<\ldots<j_{g} \leq h$ and $u_{1}=v_{j l}, u 2=$ $v_{j 2}, \ldots, u_{g}=v_{j g}$. Event sequence with length $h$ is called an $h$-sequence. Let $C=\left\{c_{1}, c_{2}, \ldots, c_{m}\right\}$ be the set of $m$ distinct classes. A labelled sequence database $D$ is a set of rows. Each row contains a sequence $s$ and its class label $c_{i}$. As an example, let we have Table 1. This table contains the labelled event sequence database $D$ with $C=\left\{c_{1}, c_{2}\right\}$. The sequence $S_{4}=C B C$ has class label $c_{1}$ and it is subsequence of the sequence $S_{2}=A C B C$ ( $S_{4} \sqsubseteq S_{2}$ ). Also we can said $S_{2}$ is supersequence of $\mathrm{S}_{4}$. The set of all sequences in $D$ which have the same class label $c_{k}$ is denoted by $D_{k}$. As an example, we have $D_{1}=\left\{S_{1}, S_{2}, S_{3}, S_{4}\right\}$ and $D_{2}=$ $\left\{S_{5}, S_{6}, S_{7}, S_{8}\right\}$.

Table 1. Labeled Event Sequence Database, D

| Sid | Sequence | Class |
| :---: | :---: | :---: |
| $S_{1}$ | $A B C C$ | $c_{1}$ |
| $S_{2}$ | $A C B C$ | $c_{1}$ |
| $S_{3}$ | $C B C$ | $c_{1}$ |
| $S_{4}$ | $B C C$ | $c_{1}$ |
| $S_{5}$ | $A B C B$ | $c_{2}$ |
| $S_{6}$ | $B C B A$ | $c_{2}$ |
| $S_{7}$ | $A B B$ | $c_{2}$ |
| $S_{8}$ | $B C B$ | $c_{2}$ |

For sequence classification, $D$ is divided into two subsets. The first set is the training dataset, $D_{\text {train }}$, to build model (Table 2) and the second set is the test dataset, $D_{\text {tess }}$, to test the model in terms of accuracy (Table 3). The set of all sequences in $D_{\text {train }}$ which have
the same class label $c_{k}$ is denoted by $D^{k}{ }_{\text {train. }}$ As an example, we have $D_{\text {tani }}^{1}=\left\{S_{1}, S_{2}, S_{3}\right\}$ and $D_{\text {tain }}^{2}=\left\{S_{5}, S_{6}\right.$, $\left.S_{7}\right\}$.

Table 2. The Training Dataset of $D, D_{\text {train }}$

| Sid | Sequence | Class |
| :---: | :---: | :---: |
| $S_{1}$ | $A B C C$ | $c_{1}$ |
| $S_{2}$ | $A C B C$ | $c_{1}$ |
| $S_{3}$ | $C B C$ | $c_{1}$ |
| $S_{5}$ | $A B C B$ | $c_{2}$ |
| $S_{6}$ | $B C B A$ | $c_{2}$ |
| $S_{7}$ | $A B B$ | $c_{2}$ |

Table 3. The Test Dataset of $\boldsymbol{D}, \boldsymbol{D}_{\text {test }}$

| Sid | Sequence | Class |
| :---: | :---: | :---: |
| $S_{4}$ | $B C C$ | $c_{1}$ |
| $S_{8}$ | $B C B$ | $c_{2}$ |

Problem Definition: Given the training sequence dataset $D_{\text {train }}$ and a new sequence with unknown class label $S_{\text {new }}$. The objective is to construct an efficient classifier (model) to classify $S_{\text {new }}$ in which the classification accuracy is high, the total response time is responsible, and the count of utilized patterns is small as possible.

## 3. RELATED WORK

The sequence classification is considered an essential data mining task. In the literature, several algorithms have been proposed for this problem. Recall, based on the used strategy for designing the model (classifier), current algorithms of sequence classification can be partitioned into three types as follows. The first type is the feature-based algorithms, the second type is the distance-based algorithms, and finally, the third type is the model-based algorithms. In this paper, we focus in the feature-based algorithms. More details about them are listed as follows.

In feature-based algorithms, each sequence is converted to a vector therefore the current algorithms of vector data classification methods will be used such as Naive Bayes, k-nearest neighbours, decision trees, hidden Markov models, support vector machines, etc. [6].

To classify sequences, the authors of [7] used the sequential patterns with Naive Bayes classification. They proposed the FeatureMine algorithm (called BayesFM) to efficiently construct the features from the sequence dataset. The main disadvantage of this method, in large feature space, the algorithm could not effectively construct the discriminative features. The Classify-By-Sequence algorithm (CBS) [8] was proposed to classify large sequences. This algorithm mines classifiable sequential patterns (CSPs) from the sequences. Thereafter, based on a scoring function, it assign a score to the new object for each class. Authors of [9] proposed a direct sequential pattern algorithm (BIDE-Discriminative) which uses class information for direct mining of predictive sequential patterns.

SeqDT [5] is a new feature-based classification algorithm which is a tree-based sequence. This algorithm. It constructs a decision tree over the feature space of all subsequences on the training set. In this algorithm, two data mining tasks are combined namely, sequential pattern mining and decision tree. In other words, it uses the methods of sequential pattern mining to mine features for the tree-based sequence classification. There are many disadvantages of SeqDT as follows. Firstly, SeqDT consumes a lot of time because it is two-phases procedure in which the feature construction and decision tree construction are two consequent phases. Secondly, many parameters are determined as input for SeqDT such as $g$ (gap constraint), $d$ (tree depth), maxL (maximum pattern length), minS (minimum value of decreased impurity generated by segmentation), threshold $\epsilon$ (maximum value of Gini index in each node), and $\operatorname{minN}$ (minimum number of sequences in each node). More details about these parameters are listed in [5]. Unfortunately, setting the values of these parameters is not simple task since each application domain may need a specific setting. In contrast, as we will see our proposed efficient method is a free-parameter method.

## 4. EVENT SEQUENCE CLASSIFICATION USING BIGSEQ

First, we discuss the construction of Big Sequence (BigSeq) as follows. The BigSeq method was proposed in our previous paper [4] to summarize the event sequence database. The main idea of BigSeq is to merge all sequences into compact big sequence. The construction of BigSeq is based on two
definitions (the longest common subsequence and the novel compatible event set). We review the construction of BigSeq using the following running example.

Example 4.1. Given the labeled event sequence dataset $D_{\text {train }}=D_{\text {train }}^{l} \cup D_{\text {train }}^{2}$ in Table 2. To construct BigSeq according to $D_{\text {train }}^{I}=\left\{S_{1}, S_{2}, S_{3}\right\}$ (Recall, all sequences in $D_{\text {train }}^{i}$ have class label equals to $c_{i}$ ). First, we randomly select any sequence $S \in D^{l}{ }_{\text {train }}$ as initial value of BigSeq. Suppose $S=S_{l}$ then the initial BigSeq is $S_{l}=A B C C$. After that, for each remaining sequence $S^{\prime} \in D_{t r a i n}^{l}-S_{1}$, we compute $\operatorname{LCS}\left(S^{\prime}\right.$, BigSeq) and store every remaining event $e$ where $e \in$ $S^{\prime}$ and $e \notin L C S\left(S^{\prime}\right.$, BigSeq). For instance, the longest common subsequences $\operatorname{LCS}\left(S_{2}\right.$, BigSeq $)$ and $\operatorname{LCS}\left(S_{3}\right.$, BigSeq) are $A C C$ and $C C$ respectively. Also, for the sequences $S_{2}$ and $S_{3}$, the set of remaining events are $\{B\}$ and $\{B\}$ respectively. Based on the remaining events of all remaining sequences, we compute the compatible event sets (core). Here, in this example, we have only one compatible event set core $_{1}$, i.e. core $=\left\{\right.$ core $\left._{1}\right\}=\{\{B, B\}\}$. Thereafter, we compute the representative event, $e_{\text {rep }}$, for core $_{1}$ and insert it in BigSeq according to the expected range of positions. Here, $e_{\text {rep }}$ is the event $B$. As result, the final Big Sequence of $D_{\text {train, }}^{l} \operatorname{Big} \operatorname{Seq}\left(D_{\text {train }}^{l}\right)$, is $A B C B C$. With the same steps, we can find the final Big Sequence of $D_{\text {train, }}^{2} \operatorname{BigSeq}\left(D_{\text {train }}^{2}\right)$. We have $\operatorname{BigSeq}\left(D_{\text {train }}^{2}\right)=$ $A B C B A$. For more details about the compatible event sets, the expected range of positions, and the construction of BigSeq, please read our previous paper [4].

Before the discussion of sequence classification using BigSeq, we illustrate how to query BigSeq.

### 4.1. Querying BigSeq

To check that a given subsequence $s$ belongs to a sequence $S(S \in D)$ or not, we can do this by checking the $\operatorname{Big}$ sequence of $D(\operatorname{BigSeq}(D))$ againt the subsequence $s$ with respect to the next two theorems.

Theorem 4.1 Given event sequence database $D$, its $\operatorname{Big} \operatorname{Sequence} \operatorname{BigSeq}(D)$, and subsequence $s$. If $s \nsubseteq \operatorname{BigSeq}(D)$ then $s \not \ddagger S \forall S \in D$.

Example 4.2 Given the training dataset $D_{t r a i n}^{l}$ in Table 2, its Big Sequence $\operatorname{BigSeq}\left(D_{\text {train }}^{t}\right),=A B C B C$, and the
subsequence $s=B B B$. Based on Theorem 4.1, we have $s=B B B \nsubseteq A B C B C=\operatorname{BigSeq}\left(D^{l}{ }_{\text {train }}\right)$, then $s \nsubseteq S$ $\forall S \in D^{l}{ }_{\text {train }}$.

Theorem 4.2 Given event sequence database $D$, its $\operatorname{Big}$ Sequence $\operatorname{BigSeq}(D)$, and subsequence $s$. If $s \sqsubseteq \operatorname{BigSeq}(D)$ then either $s \sqsubseteq S$ where $S \in D$ or $s \nsubseteq S \forall S \in D$.

Example 4.3 Given the training dataset $D_{\text {train in }}^{l}$ Table 2, its Big Sequence $\operatorname{BigSeq}\left(D_{\text {train }}^{I}\right),=A B C B C$, and the subsequence $s=A B C$. Based on Theorem 4.2, we have $s=A B C \sqsubseteq A B C B C=\operatorname{BigSeq}\left(D_{\text {train }}^{l}\right)$ with $s=$ $A B C \sqsubseteq A B C=S_{1}$ and $s=A B C \sqsubseteq A C B C=S_{2}$. In other hand, if we have another subsequence $s^{\prime}=A B B \sqsubseteq$ $A B C B C=\operatorname{BigSeq}\left(D_{\text {train }}^{l}\right)$ but $s^{\prime} \nsubseteq S \forall S \in D^{l}{ }_{\text {train }}$.

If the subsequence $s \nsubseteq \operatorname{BigSeq}(D)$ then we sure that $s \not \ddagger S$ for each $S \in D$ (Theorem 4.1). In the other hand, if $s \sqsubseteq \operatorname{BigSeq}(D)$ then either $s \sqsubseteq S$ where $S \in D$ or $s \not \ddagger S \forall S \in D$ (Theorem 4.2). In this case to prove that $s \sqsubseteq S$ where $S \in D$ or not, we can check the bitvectors of $s$ event's in $\operatorname{BigSeq}(D)$ by performing the Anding operation on the corresponding bits in these bit-vectors. If the result contains one bit equals to one then $s \sqsubseteq S$ where $S \in D$ otherwise $s \nsubseteq S \forall S \in D$. See next example for more details.

Example 4.4 Given the training dataset $D^{l}{ }_{t r a i n}$ in Table 2, its Big Sequence $\operatorname{BigSeq}\left(D_{\text {train }}^{l}\right)$, $=A B C B C$, and the two subsequences $s=A B C$ and $s^{\prime}=A B B$.
For the subsequence $s=A B C$, we have $\mathrm{s} \sqsubseteq$ $\operatorname{BigSeq}\left(D_{\text {train }}^{l}\right)$ and it has three occurrences in $\operatorname{BigSeq}\left(D_{\text {train }}^{l}\right)$ with positions $\{1,2,3\},\{1,2,5\}$, and $\{1,4,5\}$. Next we separately discuss each occurrence.

1- For the first occurrence, we perform the Anding operation on bit-vectors that fall on positions 1,2 , and 3 in $\operatorname{BigSeq}\left(D^{t}{ }_{\text {train }}\right)$. The output is 00000011 $\& 00000001 \& 00000111=00000001$. The output bit-vector has one at position 1 (i.e. it is not NULL). This means that $s$ is contained in the sequence, $S_{l}\left(s \sqsubseteq S_{l}\right)$.

2- For the second occurrence, we perform the Anding operation on bit-vectors that fall on positions 1, 2, and 5 in $\operatorname{BigSeq}\left(D^{t}{ }_{\text {train }}\right)$. The output is 00000011 \& 00000001 \& $00000111=$ 00000001 . The output bit-vector has one at position 1. This means that $s$ is contained in the sequence, $S_{I}\left(s \subseteq S_{I}\right)$. From the first and the
second occurrences of $s$ in $\operatorname{BigSeq}\left(D_{\text {train }}^{l}\right)$, we have also two occurrences of $s$ in the sequence $S_{I}$ which are $\{1,2,3\}$ and $\{1,2,4\}$.

3- For the third occurrence, we perform the Anding operation on bit-vectors that fall on positions 1, 4, and 5 in $\operatorname{BigSeq}\left(D_{\text {train }}^{l}\right)$. The output is 00000011 $\& 00000110 \& 00000111=00000010$. The output bit-vector has one at position 2. This means that $s$ is contained in the sequence, $S_{2}\left(s \sqsubseteq S_{2}\right)$.

Note that from the first and the second occurrences of $s$ in $\operatorname{BigSeq}\left(D^{l}{ }_{\text {train }}\right)$, we have $s \sqsubseteq S_{l}$. Therefore, $s$ has two occurrences in $S_{l}$. But, from the third occurrence, s has only one occurrence in $S_{2}$.

## Algorithm 1: Querying BigSeq(D)

Input: The corresponding $\operatorname{BigSeq}(D)$ with bit vectors sets of $D$ and the query subsequence $s_{q}$.
Output: $W \subseteq D$ such that $s_{q} \subseteq S$ for each $S \in W$ otherwise NULL.

1. if $s_{q} \not \equiv \operatorname{BigSeq}(D)$ then // Theorem 4.1
2. return NULL
. end if
3. else // Theorem 4.2
4. Find the set of all occurrences of $s_{q}$ in $\operatorname{BigSeq}(D)$, $O\left(s_{q}\right)$.
for each occurrence $o \in O\left(s_{q}\right)$ do
5. Suppose $p_{l}, p_{2}, \ldots, p_{\mid S_{q \mid}}$ be the positions of $o$ in $\operatorname{BigSeq}(D)$.
6. Compute B_output $=B\left(e p_{l}\right) \& B\left(e p_{2}\right) \& \ldots \&$ $\mathrm{B}\left(\mathrm{e} p_{\left|S_{q}\right|}\right) \quad / / e p_{i}$ is the event $e$ at position $p_{i}$ in $\operatorname{BigSeq}(D)$.
7. for each $B_{i} \in B$ _output do
8. for $j=1$ to 8
if $B_{i}[j]=1$
$W=W \cup S_{8 \times(i-l)+j}$
end if
end for
end for
end for return $W$

For the subsequence $s^{\prime}=A B B$, we have $s^{\prime} \sqsubseteq$ $\operatorname{BigSeq}\left(D_{\text {train }}^{I}\right)$ and $s^{\prime}$ has only one occurrence in $\operatorname{BigSeq}\left(D_{\text {train }}^{I}\right)$ with position $\{1,2,4\}$. Therefore, we perform the Anding operation on bit-vectors that fall on positions 1, 2, and 4 in $\operatorname{BigSeq}\left(D^{l}{ }_{\text {train }}\right)$. The output is $00000011 \& 00000001 \& 00000110=00000000$.

The output bit-vector has no ones (i.e. it is NULL). This means that $s^{\prime} \nsubseteq S \forall S \in D$ and at the same time, we have $s^{\prime}$ ㄷigSeq( $\left.D^{l}{ }_{\text {train }}\right)$.

Algorithm 1 outlines the process of querying $\operatorname{BigSeq}(D)$. The input of this algorithm is the big sequence of $D, \operatorname{BigSeq}(D)$, and the query subsequence $s_{q}$ while the output is the set of sequences in $D$ that contains $s_{q}$ denoted as $W$. Lines 1-2 apply Theorem 4.1 that is if $s_{q} \nsubseteq \operatorname{BigSeq}(D)$ then returns NULL. Lines 4-16 apply Theorem 4.2 as follows. First, we find the set of all occurrences of $s_{q}$ in $\operatorname{BigSeq}(D)$. denoted as $O\left(s_{q}\right)$. Second, for each occurrence $o=\left\{p_{1}, p_{2}, \ldots, p_{\left|s_{q}\right|}\right\}$ in $O\left(s_{q}\right)$, we Anding the bit vectors of the events $e p_{1}, e p_{2}, \ldots, \mathrm{e} p \mid S_{q \mid}$ in $\operatorname{BigSeq}(D)$, where $e p_{i}$ is the event $e$ at position $p_{i}$. We denote the output of the Anding operation as $B_{-}$output. Note that $B_{-}$output is a set of bit-vectors, $B_{-}$output $=\left\{B_{1}, B_{2}, \ldots, B_{m}\right\}$, where the length of $B_{i}$ is 8 bits and $m=D / 8$. Finally, for each block $B_{i} \in$ $B_{-}$output, if there exist any bit in any $B_{i}$ equals to 1 , we add its corresponding sequence to $W$.

### 4.2. Classification Method

In this section, we discuss the event sequence classification using BigSeq method. Recall, for event sequence classification, $D$ is divided into two subsets. The first set is the training set $D_{\text {train }}$ (to build the model) and the second set is the test set $D_{\text {test }}$ (to test the model in terms of accuracy). To build the proposed model using BigSeq, we divide $D_{\text {train }}$ into $m$ subsets where $m$ is the number of classes in the dataset ( $m=|C|$ ) such that each subset will have the same class label. For each subset $D_{\text {train }}^{i}$ (Note that each sequence $S \in D_{\text {train }}^{i}$ has class label ci such that $i=1$, $\ldots, m$ ), we construct its Big Sequence, $\operatorname{BigSeq}\left(D_{\text {train }}^{i}\right)$. As a result, our model will be represented by $m$ BigSeqs. Based on our model, to classify a new sequence $S_{\text {new }}$ with unknown class label, we have two cases as follows. In the first case, if $S_{\text {new }}$ is not subsequence of $\operatorname{BigSeq}\left(D_{\text {train }}^{i}\right)$. for all $i=1, \ldots, m$ (Theorem 4.1), we compute $\operatorname{LCS}\left(S_{\text {new }}, \operatorname{BigSeq}\left(D_{\text {train }}^{i}\right)\right.$ ) for each $\operatorname{BigSeq}\left(D_{\text {train }}^{i}\right)$ in our model where $i=1, \ldots$, $m$. Thereafter, we search for the maximum length of $L C S$ among all BigSeqs. Suppose $L C S\left(S_{\text {new }}\right.$, $\operatorname{BigSeq}\left(D_{\text {train }}^{k}\right)$ ) has the maximum value then we label $S_{\text {new }}$ by $c_{k}$. In the second case, if there exist index $k$ such that $S_{\text {new }}$ is subsequence of $\operatorname{BigSeq}\left(D^{k}{ }_{\text {train }}\right)$ then we simply label $S_{\text {new }}$ by $c_{k}$ and we do not search for the occurrences of $S_{\text {new }}$ in $\operatorname{BigSeq}\left(D_{\text {train }}^{k}\right)$ to save a
time. In Experimental Evaluation section, we test the performance of our classification method on real datasets with respect to classification accuracy, total response time, and count of utilized patterns. Algorithm 2 outlines the construction of our model and the classification of a new sequence $S_{\text {new }}$ with unknown class label.

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Algorithm 2: Model Construction \& Sequence Classification
Input: The training dataset \(D_{\text {train }}\) and the new sequence \(S_{\text {new }}\) with unknow class label.
Output: The class label of \(S_{\text {new }}\)
1. Divide \(D_{\text {train }}\) into \(m\) subsets based on the class label \(c_{i}\left(D_{\text {train }}=\bigcup_{i=1}^{m} D_{\text {train }}^{i}\right)\)
2. for each \(i=1\) to \(m\) do
3. Construct the Big Sequence \(\operatorname{Big} \operatorname{Seq}\left(D_{\text {train }}^{i}\right)\)
4. Arr_W \([i]=\operatorname{Querying}\left(\operatorname{BigSeq}\left(D_{\text {train }}^{i}\right), S_{\text {new }}\right) / /\) Call Algorithm 1
5. end for
6. if \(A r r_{-} W[i]=\) NULL \(\forall i=1, \ldots, m / /\) Theorem 4.1
7. for each \(i=1\) to \(m\) do
8. Compute \(L C S^{i}=\operatorname{LCS}\left(S_{\text {new }}, \operatorname{BigSeq}\left(D_{\text {train }}^{i}\right)\right)\)
9. end for
10. \(k=\operatorname{argmax}_{i=1 \ldots m} L C S^{i}\)
11. Label \(S_{\text {new }}\) by \(c_{k}\)
12. end if
13. else
14. Find the index \(k\) where \(A r r_{-} W[k] \neq\) NULL
15. Label the sequence \(S_{\text {new }}\) by \(c_{k}\)
```


## 5 EXPERIMENTAL EVALUATION

This section shows the results of experiments on three real datasets. We compare our proposed algorithm, CBigSeq, with SeqDT algorithm [5] (the state-of-the-art algorithm). Note that, we used SeqDT in our experiments beacuse it outperforms the four algorithms SEQL [10], MiSeRe [11], Sqn2Vec [12], and SCIP [13].

CBigSeq was implemented in C++ with STL library and compiled with GNU GCC while the code of SeqDT was downloaded from https://github.com/ZiyaoWu/SeqDT. Experiments were run on laptop (Intel i3 2.4 GHz and 8 G memory) running Linux. The three datasets are reported in the next section.

Table 4. Summary Statistics of the Real Datasets used in Our Experiments

| Dataset | $\|\mathcal{D}\|$ | $\|E\|$ | $\min L$ | $\max L$ | avg_L | \#classes |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Question | 1731 | 3612 | 4 | 29 | 10.17 | 2 |
| Poineer | 160 | 178 | 4 | 100 | 40.14 | 3 |
| Gene | 2942 | 5 | 41 | 216 | 86.53 | 2 |

### 5.1 Datasets

To evaluate our proposed algorithm, CBigSeq, we used three real datasets namely, Question [14], Poineer [9], and Gene [15]. These datasets are summarized in Table 4, where $|D|$ is the number of event sequences, $|E|$ represents the count of the events, min_L, max_L, avg_L, and \#classes represent the minimum length, the maximum length, the average length, and the number of distinct classes of the event sequences respectively. Also, Table 5 reports URLs of the used datasets.

Table 5. URLs of the Real datasets Used in Our Experiments

| Dataset | URL |
| :---: | :---: |
| Question | http://cogcomp.cs.illinois.edu/Data/QA/QC/ |
| Poineer | http://archive.ics.uci.edu/ml/datasets/Pioneer-1+Mobile+Robot+Data |
| Gene | http://datamining.xmu.edu.cn:8080/miRNApre- |

### 5.2 Performance of CBigSeq against SeqDT

CBigSeq algorithm is evaluated based on the following three criteria:

1. Accuracy: To measure the accuracy of our model.
2. Total Response Time: To measure the efficiency of CBigSeq.
3. The Count of Utilized Patterns: To show the count of utilized patterns for classification.

### 5.2.1 Accuracy

In this section, we discuss the accuracy (\%) of the two algorithms on the three datasets. For each dataset, we select a number of sequences for training and other number of sequences for testing as in Table 6.

Table 6. Train and Test Sequences for each Dataset

| Dataset | Train Sequences | Test Sequences |
| :---: | :---: | :---: |
| Question | 1493 | 238 |
| Poineer | 129 | 31 |
| Gene | 2354 | 588 |

Table 7 reports the accuracy (\%) of the two algorithms. From this table, CBigSeq shows higher
accuracy than SeqDT Question dataset whereas the opposite occurs on the Pioneer dataset. On Gene dataset, the two algorithms have the same accuracy (100\%).

Table 7. Accuracy (\%) of the two algorithms (CBigSeq against SeqDT)

| Dataset | CBigSeq | SeqDT |
| :---: | :---: | :---: |
| Question | $99.5 \%$ | $96.6 \%$ |
| Poineer | $80.6 \%$ | $100 \%$ |
| Gene | $100 \%$ | $100 \%$ |

Figure 1 reports the scalability test (the number of training sequences) of CBigSeq against SeqDT in terms of accuracy. This scalability test was done on the Question dataset with 238 sequences for testing. From this Figure, CBigSeq algorithm shows a better accuracy when the number of train sequences are 1000 and 1200 . For example, with 1200 sequences for training, the accuracy of CBigSeq is $96.6 \%$ while the accuracy of SeqDT is $95.3 \%$. On the other hand, SeqDT has a better accuracy when the number of train sequences are 900 and 1100. For example, with 900 sequences for training, the accuracy of SeqDT is $94.5 \%$ while the accuracy of CBigSeq is $94.1 \%$.

Recall, many parameters are determined as input for SeqDT such as the two parameters $g$ (the gap constraint) and $d$ (the tree depth) whereas our proposed algorithm CBigSeq is free-parameters. Therefore, in the next experiment, we show the parameter sensitivity of SeqDT in terms of accuracy while our proposed algorithm, CBigSeq, is stable. This experiment was done on Question dataset with 1200 sequences for training and 238 sequences for testing. We selected values for $g$ and $d$ as follows. The values of $g$ are $1,2,3,4$, and 5 whereas the values of $d$ are 2, 5, 7, 9, and 11. In Figure 2, for gap constraint $(g)$, the accuracy of CBigSeq is stable and equals to $96.6 \%$ while the accuracy of SeqDT is not stable and falls on the range from $93.69 \%$ to $95.37 \%$. In Figure 3 , for tree depth ( $d$ ), the accuracy of CBigSeq is also stable and equals to $96.6 \%$ while the accuracy of SeqDT is not stable and falls on the range from $83.19 \%$ to $95.37 \%$.


Figure 1. Scalability Test (Accuracy)


Figure 2. Gap Constraint (Accuracy)


Figure 3. Tree Depth (Accuracy)

### 5.2.2 Total Response Time

In this experiment, the number of sequences for training and testing is the same as in the previous section (see Table 6). Table 8 reports the total response time (MSec) of the two algorithms on the three datasets. From this table, on Question dataset, CBigSeq outperforms SeqDT by three factors. On Pioneer dataset, the two algorithms have approximately the same time. While, on Gene dataset, SeqDT outperforms CBigSeq by more than two factors.

Table 8. Total Response Time (MSec) of the two algorithms (CBigSeq against SeqDT)

| Dataset | CBigSeq | SeqDT |
| :---: | :---: | :---: |
| Question | 343 | 1085 |
| Poineer | 215 | 223 |
| Gene | 1523 | 593 |

Figure 4 reports the scalability test (the number of training sequences) of CBigSeq against SeqDT with respect to total response time (MSec). This scalability test was done on the Question dataset with 238 sequences for testing. From this Figure, CBigSeq algorithm shows the best performance. In other words, BigSeq outperforms SeqDT by more than three factors.

Now, we test the parameter sensitivity of SeqDT in terms of total response time while the proposed algorithm, CBigSeq (free-parameters) is stable. This experiment was done on Question dataset with 1200 sequences for training and 238 sequences for testing. As in previous section, we also used the two parameters $g$ (the gap constraint) and $d$ (the tree depth) with the same selected values. In Figure 5, for gap constraint ( $g$ ), the total response time of CBigSeq is stable and equals to 343 MSec while the total response time of SeqDT is not stable and falls on the range from 1027 MSec to 1684 MSec . In other words, BigSeq outperforms SeqDT by more than five factors. In Figure 6, for tree depth (d), the total response time of
CBigSeq is also stable and equals to 343 MSec while the total response time of SeqDT is not stable and falls on the range from 810 MSec to 1027 MSec . In other words, BigSeq outperforms SeqDT by more than three factors.


Figure 4. Scalability Test (Total Response Time)


Figure 5. Gap Constraint (Total Response Time)


Figure 6. Tree Depth (Total Response Time)

### 5.2.3 The Count of Utilized Patterns

Table 9 shows the count of utilized patterns for classification by the two algorithms on the three datasets. Note that CBigSeq utilized only $|C|$ patterns i.e. $|C|$ BigSeqs (Recall, $|C|$ is the number of classes in the running dataset) for all datasets. In the Question dataset, the count of utilized patterns of CBigSeq is smaller than SeqDT. This means that our proposed method constructs an efficient model for classification with only a small number of patterns. In the other two datasets, Pionner and Gene, the two algorithms CBigSeq and SeqDT construct their models by approximately the same count of utilized patterns.

Table 9. The Count of Utilized Patterns of the two algorithms (CBigSeq against SeqDT)

| Dataset | CBigSeq | SeqDT |
| :---: | :---: | :---: |
| Question | 2 | 35 |
| Poineer | 3 | 3 |
| Gene | 2 | 1 |

## 6 CONCLUSION

In this paper, we focus on classification event sequence dataset. Existing algorithms of sequence classification are partitioned into three types (featurebased, distance-based, and model-based algorithms). Here, we proposed a feature-based algorithm called CBigSeq. CBigSeq is based on the idea of compact big sequence (BigSeq). Our model contains a set of BigSeqs such that each BigSeq in our model represents a subset of training sequences that have the same class label. Via an extensive evaluation on three real datasets, we show that CBigSeq outperforms the state-of-the-art competitor, SeqDT, in most cases in terms of classification accuracy, total response time, and count of utilized patterns.

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## Conflicts of Interest

The author declares that I don't have any conflict of interest regarding this article.

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